#### Phenomenology of Particle Dark Matter

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PhD Completion Seminar March 10th, 2017

Featuring work with Nicole Bell, Yi Cai, Tom Weiler, James Dent, Kenny Ng and John Beacom







We don't know what

# **95**%

#### of the universe is!

#### The rest is "dark" stuff.

#### Dark matter, and dark energy.























Bullet Cluster Chandra X-Ray Telescope Hubble Space Telescope

#### Abundance of evidence



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Phenomenology of Particle Dark Matter

- There is overwhelming evidence that dark matter is the dominant form of matter in the universe, yet little is known about its physical properties.
- To better understand our universe at a fundamental level, it is necessary to develop theories which can be correctly probed at experiments.

#### Searches for particle dark matter

- WIMP dark matter well motivated: weak scale masses and interaction strengths
- Realistic detection prospects



#### Effective field theories for dark matter



- Model independent
- Useful at low energies, i.e. direct detection
- Colliders? Need to be careful. Cutoff at new physics scale.

• In the Standard Model, electroweak symmetry is broken by Higgs mechanism, giving rise to longitudinal modes. Allows masses for *W* and *Z* gauge bosons.

 $SU(3) \otimes SU(2)_L \otimes U(1)_Y \rightarrow SU(3)_C \otimes U(1)_{QED}$ 

- Any breaking of electroweak symmetry is linked to the "scale" of the Higgs field, called the "vev"
- If an EFT does not respect the electroweak gauge symmetries of the SM, it may be invalid around the electroweak scale, rather than the scale of new physics.

$$\frac{\mathsf{vev}^2}{\Lambda^4} (\overline{\chi} \gamma^\mu \chi) (\overline{u}_L \gamma_\mu u_L)$$

#### Mono-X signal at colliders

- $\bullet\,$  Dark matter  $\to\,$  missing energy in the detector
- Visible matter recoils against this missing energy
- Examples include mono-Z, mono-W, mono-photon, mono-jet

 $pp \rightarrow \overline{\chi}\chi + SM$  particle

 $pp \rightarrow \mathrm{MET} + \mathrm{SM}$  particle





#### ATLAS experiment, CERN

# Mono-W EFT



$$\frac{1}{\Lambda^2}(\overline{\chi}\gamma^{\mu}\chi)(\overline{u}\gamma_{\mu}u+\xi\overline{d}\gamma_{\mu}d)$$

- Theorists set  $\xi \neq +1$ , claimed to find "interference effect"
- Analysis was repeated by ATLAS and CMS

# Mono-W EFT



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# **UV** Completion





#### Longitudinal effects





- Cross section first suppressed due to increase in propagator mass, then increases when third diagram begins to dominate
- However, enforcing gauge invariance and perturbativity, this effect can't be large

N. Bell, Y. Cai, RKL, 1512.00476

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March 10th, 2017 26 / 50

## Generic simplified models for mono-W signal

#### t-channel colored scalar:



#### s-channel Z':





Consider both:

- Mono-lepton channel
- Mono-fat jet channel

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#### t-channel LHC limits and reach summary



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#### s-channel LHC limits and reach summary



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29 / 50

#### s-channel LHC limits and reach summary



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30 / 50

# Implications of gauge invariance in other searches?

#### Simplified models for dark matter

- Still no idea about fundamental nature of DM, model independent framework desirable where possible
- EFTs  $\rightarrow$  issues at high momentum transfer, not generically applicable
- Simplified models: only lightest mediator is retained, set limits on couplings and mediators. Allow for richer phenomenology.

#### Benchmark Simplified Models:



- Not intrinsically capable of capturing full phenomenology of UV complete theories
- Separate consideration of these benchmarks can lead physical problems and inconsistencies
  - Results may not map to any viable model!
- To avoid this, important to consider minimal ingredients of gauge invariant models, ensuring valid interpretation of experimental data

#### Issues with Spin-1 Simplified Models

Common model is  $SM \otimes U(1)_{dark}$ . Consider the high energy production of longitudinal Z' bosons:



violates unitarity at high energies, for axial-vector Z'-DM couplings. Kahlhoefer et al, 1510.02110

#### Issues with Spin-1 Simplified Models

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Consequences for both Majorana and Dirac DM.

For Majorana DM, vector current is vanishing, leaving pure axial-vector interactions.

\*\* Inclusion of the dark Higgs is unavoidable! \*\*

Furthermore, can't write down Majorana mass term without breaking the  $U(1)_{\mathrm{dark}}$  symmetry.

New fields:

- Majorana DM candidate,  $\chi$
- Spin-1 dark gauge boson, Z',
- Dark Higgs field, S.
- S obtains a vev to give mass to  $\chi$  and Z'
- U(1) charges of  $\chi$  and S related by gauge invariance:  $Q_S = 2Q_{\chi}$
- Parameters tied together:  $y_\chi/g_\chi=\sqrt{2}m_\chi/m_{Z'}$

# Annihilation Processes: Standard Simplified Models

- To investigate phenomenology, focus on hidden sector models, where couplings to SM are small
- In universe today, only s-wave contributions to the annihilation cross section are relevant. P-wave contributions are negligible, suppressed as DM velocity  $v_{\chi}^2 \approx 10^{-6}$



# What happens when we consider the self-consistent dark sector?

#### Annihilation Processes: Self-Consistent Scenario

N. Bell, Y. Cai, R. Leane, 1605.09382



New addition to  $\chi\chi \rightarrow Z'Z'$  process.



New s-wave annihilation process!

Further, this allows us to probe the nature of the scalar with comparable strength to the Z'.

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#### Annihilation Processes: Comparison



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March 10th, 2017 40 / 50

## Indirect Detection Limits

- Best limits from Dwarf Spheriodal Galaxies, most DM dense objects in our sky
- Use **Pythia** to generate gamma-ray spectra, compare to Fermi Pass 8 data and find limits



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41 / 50

## Linked to Dark Sector Mass Generation

#### Majorana DM:

- Pure axial-vector couplings to Z'
- Both DM and Z' masses arise from dark Higgs mechanism

#### Dirac DM:

- Both vector and axial-vector couplings possible
- If Z' has pure vector couplings:
  - Z' mass: either Higgs or Stueckelberg mechanism
  - DM mass: bare mass or Higgs mechanism
  - Mass generation mechanisms not necessarily connected
- If Z' has non-zero axial couplings:
  - Dark Higgs gives mass to both Z' and DM (like Majorana)

- Correctly enforcing gauge invariance is key for DM models, leads to important phenomenology missed in "over-simplified" model approach
- Another important avenue is finding distinctive new signatures, exploiting strengths of different experiments

DM can be captured in the Sun by scattering with solar nuclei.

- Of possible DM annihilation modes, only neutrinos weakly interacting enough to escape
- These neutrinos are measured at SuperK and IceCube, provide probe of DM scattering cross section
- What if DM annihilates to long-lived mediators instead?

# Solar Signatures of Long-lived Dark Mediators

If annihilation proceeds via long-lived dark mediators:

- Neutrinos will be less attenuated
- Other particles such as gamma-rays can escape



45 / 50

## Measuring gamma-rays with new Fermi-LAT data

Standard annihilation fluxes of DM to gamma-rays are enormous. For example, if 100 GeV DM with scattering  $\sigma_{\chi P}^{SD} \sim 10^{-40} \, {\rm cm}^2$  annihilates directly to gamma-rays, the energy flux is

$$\sim 10^{-4} \, {\rm GeV} \, {\rm cm}^{-2} \, {\rm s}^{-1}.$$

In this region, the sensitivity of Fermi-LAT is

$$\sim 10^{-8} \, {\rm GeV} \, {\rm cm}^{-2} \, {\rm s}^{-1}.$$

The annihilation flux is in excess of sensitivity by a factor of 10,000!

 $\rightarrow$  Long-lived mediators open a window to otherwise lost DM signals, potentially large rates!

RKL, K. Ng, J. Beacom (to appear)

#### DM scattering cross section limits: Gamma-rays

Can outperform direct detection exps by several orders of magnitude!



#### DM scattering cross section limits: Neutrinos

Outperforms both direct detection exps and neutrino telescopes



Understanding the nature of DM is one of the foremost goals of the physics community. Important steps forward for discovery include:

#### Theoretically consistent models:

- EFT consistency, LHC mono-W enhancements not possible
- Single mediator Simplified Models not always self-consistent
- Two mediators can be required by gauge invariance
  - Leads to different phenomenology
  - ▶ New s-wave process, which dominates the annihilation rate

#### New ways of exploiting complementarity of DM searches:

- DM annihilation to long-lived mediators in the Sun provides probe of DM scattering cross section
- Can outperform direct detection exps by several orders of magnitude

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  - Nicole Bell, Ray Volkas, Andrew Melatos
- Other mentors
  - John Beacom, Tom Weiler, Matt Dolan
- CoEPP and the School of Physics

# **Backup slides**

#### Gamma-rays:

- Current limits use Fermi data on solar gamma-rays
  - 2011 and 2015 analyses
- Future sensitivity with water cherenkov telescopes HAWC and LHAASO
  - ▶ HAWC has data, sensitive to very high (>TeV) gamma-rays
  - LHAASO upcoming, also extremely sensitive to very high (>TeV) gamma-rays

Neutrinos:

- Best gain for long-lived mediators is at higher (>TeV) energies
  - Less neutrino absorption by the solar matter
  - Less cooling of the secondaries (pions, muons etc)
- Use gigaton neutrino telescopes IceCube and KM3Net

# Long-lived dark mediator flux

$$E^2 \frac{d\Phi}{dE} = \frac{\Gamma_{\rm ann}}{4\pi D_{\oplus}^2} \times E^2 \frac{dN}{dE} \times Br(Y \to SM) \times P_{\rm surv},$$
 (1)

where

- $D_{\oplus} = 1$  A.U. is the distance between the Sun and the Earth
- $E^2 dN/dE$  is the particle energy spectrum per DM annihilation
- $Br(Y \to SM)$  is the branching fraction of the mediator Y to SM particles
- $P_{\rm surv}$  is the probability of the signal surviving to reach the detector, given by

$$P_{\rm surv} = e^{-R_{\odot}/\gamma c\tau} - e^{-D_{\oplus}/\gamma c\tau}.$$
 (2)

Need mediator Y to have sufficiently long lifetime  $\tau$  or boost factor  $\gamma = m_{\chi}/m_{Y}$ , leading to a decay length L that exceeds the radius of the Sun,  $R_{\odot}$ , as

$$L = \gamma c \tau > R_{\odot}. \tag{3}$$

#### Signal survival probability



#### Gamma-ray limit procedure



 $\chi\chi \rightarrow YY \rightarrow 2$  (SM + SM)  $\rightarrow ...\gamma...$ 

## Gamma-ray limits



#### Neutrino limit procedure



 $\chi \chi \rightarrow YY \rightarrow 2 ( SM + SM ) \rightarrow ...\nu...$ 

# Long-lived dark mediator constraints

- **BBN:** The observed relic abundance of SM particles by BBN implies any new mediator must have lifetime  $\tau$  which satisfies  $\tau < 1$ s.
- **CMB:** DM annihilation to SM products in the early universe is constrained by the CMB.
- **Supernovae:** Particularly for low mass mediators (<GeV), from mediator decay and supernova cooling.
- **Colliders:** If the dark sector is secluded, may be negligible. Otherwise, Belle, BaBar, ATLAS and CMS
- Beam Dump/Fixed Target experiments: Most relevant when the mediator has ~sub-GeV mass. E137, LSND and CHARM
- Other indirect detection signals: Fermi-LAT and DES measurements of dSphs at low DM mass, and large positron signals can be constrained by AMS-02
- Thermalization and Unitarity: Issues with thermalization for > 10 TeV DM, and unitarity issues over  $\mathcal{O}(100)$  TeV DM mass. Furthermore bound state effects at high DM mass.



New fields: Majorana DM candidate,  $\chi$ , Spin-1 dark gauge boson, Z', Dark Higgs field S.

$$\mathcal{L} = \mathcal{L}_{\mathrm{SM}} + \mathcal{L}_{\mathrm{dark}} + \mathcal{L}_{\mathrm{mix}}$$

$$\begin{split} \mathcal{L}_{\mathrm{dark}} &= \frac{i}{2} \overline{\chi} \partial \!\!\!/ \chi - \frac{1}{4} g_{\chi} Z'^{\mu} \overline{\chi} \gamma_5 \gamma_{\mu} \chi - \frac{1}{2} y_{\chi} \left( \overline{\chi}_L^C \chi_L S + h.c. \right) \\ &+ \left( D^{\mu} S \right)^{\dagger} \left( D_{\mu} S \right) - \mu_s^2 S^{\dagger} S - \lambda_s (S^{\dagger} S)^2 \end{split}$$

- S obtains a vev to give mass to  $\chi$  and Z'
- U(1) charges of  $\chi$  and S related by gauge invariance:  $Q_S = 2Q_{\chi}$
- Parameters tied together:  $y_{\chi}/g_{\chi} = \sqrt{2}m_{\chi}/m_{Z'}$

# Impact of Specifying Mass Generation

Scenario	$\chi$ mass	Z' mass	Required $\chi - Z'$ coupling type	Annihilation processes	Z' pol
I	Bare mass term	Stueckelberg mechanism	Vector		$Z'_T$
			Non-zero axial-vector		
п	Yukawa coupling to Dark Higgs	Dark Higgs mechanism	The $U(1)$ charge assignments of $\chi_L$ and $\chi_R$ determine the relative size of the V and A couplings		Z' <sub>T</sub> & Z' <sub>L</sub>
			contringer	x	
ш	Yukawa coupling to Dark Higgs	Stueckelberg mechanism	Vector		$Z'_T$
IV	Bare mass term	Dark Higgs mechanism	Vector		$Z'_T$

#### DM and Z' Mass from Dark Higgs



- Couplings related:  $y_{\chi}/g_{\chi} = \sqrt{2}m_{\chi}/m_{Z'}$
- sZ' dominates over Z'Z' when kinematically allowed
- Cross sections enhanced by longitudinal Z' (for Z'Z' this only occurs when both vector and axial couplings are non-zero)

# DM mass from Dark Higgs, Z' mass from Stueckelberg

- Gauge and Yukawa couplings no longer related, freedom in processes
- Z' is only transversely polarized



## Bare DM Mass, Z' Mass from Stueckelberg

- Gauge and Yukawa couplings no longer related, U(1) charges of Z' and dark Higgs unrelated
- Z' is only transversely polarized



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64 / 50

# Two-Mediator Scenario: Charge Assignments

Yukawa term is

$$\mathcal{L}_{\text{Yukawa}} = -\left(y_{\chi}\overline{\chi}_{R}\chi_{L}S + h.c.\right),\tag{4}$$

and so the charges of the dark sector field must be chosen to satisfy

$$Q_{\chi_R} - Q_{\chi_L} = Q_S . \tag{5}$$

Set the dark Higgs charge to  $Q_S=1.$  The  $\chi$  charges therefore satisfy

$$Q_A \equiv \frac{1}{2}(Q_{\chi_R} - Q_{\chi_L}) = \frac{1}{2},$$
 (6)

$$Q_{V} \equiv \frac{1}{2}(Q_{\chi_{R}} + Q_{\chi_{L}}) = \frac{1}{2} + Q_{\chi_{L}}.$$
 (7)

These charges determine the vector and axial-vector couplings of the Z' to the  $\chi$ .  $Q_A$  is completely determined, while there is freedom to adjust  $Q_V$  by choosing  $Q_{\chi_{L,R}}$  appropriately.

#### Two-Mediator Scenario: Indirect Detection Constraints



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In all scenarios, the gauge group is:  $SM \otimes U(1)_{\chi}$ , and so the the covariant derivative is  $D_{\mu} = D_{\mu}^{SM} + iQg_{\chi}Z'_{\mu}$ , where Q denotes the  $U(1)_{\chi}$  charge.

#### Bare DM Mass, Z' Mass from Stueckelberg

This is the most minimal spin-1 setup, and no additional fields are introduced, as Z' obtains mass via Stueckelberg and DM is vectorlike so a bare mass term is allowed. The lagrangian is

$$\mathcal{L} = \mathcal{L}_{SM} + i\,\overline{\chi}(\partial_{\mu} + ig_{\chi}Q_{V}Z'_{\mu})\gamma^{\mu}\chi - \frac{\sin\epsilon}{2}Z'^{\mu\nu}B_{\mu\nu} - m_{\chi}\overline{\chi}\chi + \frac{1}{2}m_{Z'}^{2}Z'^{\mu}Z'_{\mu}.$$
(8)

#### Lagrangian: Scenario II

In this scenario, the vev of the dark Higgs field provides a mass generation mechanism for the dark sector fields Z' and  $\chi$ . Before electroweak and  $U(1)_{\chi}$  symmetry breaking, the most general Lagrangian is

After symmetry breaking, this becomes

$$\mathcal{L} \supset -\frac{1}{2}m_{s}^{2}s^{2} + \frac{1}{2}m_{Z'}^{2}Z'^{\mu}Z'_{\mu} - m_{\chi}\overline{\chi}\chi + g_{\chi}^{2}wZ'^{\mu}Z'_{\mu}s - \lambda_{s}ws^{3} - 2\lambda_{hs}hs(vs + wh) + g_{f}\sum_{f}Z'_{\mu}\overline{f}\Gamma_{f}^{\mu}f \quad (10) - g_{\chi}Q_{V}Z'_{\mu}\overline{\chi}\gamma^{\mu}\chi - g_{\chi}Q_{A}Z'_{\mu}\overline{\chi}\gamma^{\mu}\gamma_{5}\chi - \frac{y_{\chi}}{\sqrt{2}}s\overline{\chi}\chi .$$

#### DM Mass from Dark Higgs, Z' Mass from Stueckelberg

The most minimal Lagrangian for this scenario is

$$\mathcal{L} = \mathcal{L}_{SM} + i \overline{\chi} \left( \partial \!\!\!/ + i g_{\chi} Q_V \overline{Z}' \right) \chi - \frac{y_{\chi}}{\sqrt{2}} \overline{\chi} \chi \phi - \frac{\sin \epsilon}{2} Z'^{\mu\nu} B_{\mu\nu} \quad (11)$$
  
+  $\frac{1}{2} \partial_{\mu} \phi \partial^{\mu} \phi - \frac{1}{2} \mu_s^2 \phi^2 - \frac{1}{4} \lambda_s \phi^4 - \frac{1}{2} \lambda_{hs} \phi^2 (H^{\dagger} H),$ 

with the real scalar  $\phi = w + s$ , where w is the vev of  $\phi$  and s is the dark Higgs. The vectorlike charge  $Q_V$  can be chosen freely.

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#### Bare DM Mass, Z' Mass from Dark Higgs

The most minimal gauge invariant Lagrangian is

$$\mathcal{L} = \mathcal{L}_{SM} + i \overline{\chi} \left( \partial \!\!\!/ + i g_{\chi} Q_V \overline{Z}' \right) \chi - \frac{\sin \epsilon}{2} Z'^{\mu\nu} B_{\mu\nu} - m_{\chi} \overline{\chi} \chi \quad (12)$$
  
+ 
$$\left[ \left( \partial^{\mu} + i g_{\chi} Q_S Z'^{\mu} \right) S \right]^{\dagger} \left[ \left( \partial_{\mu} + i g_{\chi} Q_S Z'_{\mu} \right) S \right] - \mu_s^2 S^{\dagger} S$$
  
- 
$$\lambda_s (S^{\dagger} S)^2 - \lambda_{hs} (S^{\dagger} S) (H^{\dagger} H).$$

The vectorlike charge  $Q_V$  and dark Higgs charge  $Q_S$  under the dark  $U(1)_{\chi}$  can be chosen freely.
$$\sqrt{s} < rac{\pi m_{Z'}^2}{g_\chi^2 m_\chi}$$
 $m_f < \sqrt{rac{\pi}{2}} rac{m_{Z'}}{g_f^A}$ 

Parameters related, sensible choices required to avoid unitarity problems:

$$m_{Z'} = g_{\chi} w$$
 $m_{\chi} = rac{1}{\sqrt{2}} y_{\chi} w$ 
 $y_{\chi}/g_{\chi} = \sqrt{2} m_{\chi}/m_{Z'}$ 

March 10th, 2017 71 / 50

## Scalar operator:

$$\frac{m_q}{\Lambda^3} \left( \overline{\chi} \chi \right) \left( \overline{q} q \right) = \frac{m_q}{\Lambda^3} \left( \overline{\chi} \chi \right) \left( \overline{q}_L q_R + h.c. \right)$$

LH quark SU(2) doublet, DM and RH quark singlets.

**Vector operator:** 

$$\frac{1}{\Lambda^2} \left( \overline{\chi} \gamma^\mu \chi \right) \left( \overline{q} \gamma_\mu q \right) = \frac{1}{\Lambda^2} \left( \overline{\chi} \gamma^\mu \chi \right) \left( \overline{q}_L \gamma_\mu q_L + \overline{q}_R \gamma_\mu q_R \right)$$

OK provided same coefficients for each LH up and down quark.

N. Bell, Y. Cai, J.Dent, RKL, T, Weiler, 1503.07874



- Quark-Z' couplings like that of the Z, which are of opposite sign for u and d quarks due to their weak isospin assignments of T<sub>3</sub> = ±1/2. In the EFT limit, where the Z' is integrated out, this would give negative value of ξ.
- However, the strength of the DM-quark interactions would be suppressed by the Z/Z' mixing angle, which is of order  $vev^2/m_{Z'}$  and thus the operator arises only at order  $1/\Lambda^4$

N. Bell, Y. Cai, RKL, 1512.00476

Follow CMS mono-lepton search (arXiv: 1408.2745). Main background W > lv. Important kinematic variable:

$$M_T = \sqrt{2p_T^\ell \not\!\!\! E_T (1 - \cos \Delta \phi_{\ell,\nu})}$$

MC with MadGraph, Showering with Pythia, Detector effects with Delphes / Fastjet. Run two regions, with low pt and high pt cuts



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- $E_T$  of the leading electron > 100 GeV
- $E_T$  of the next-to-leading electron < 35 GeV
- At least one electron
- $M_T$  for the electron,  $M_T^e > 220$  GeV
- Pseudorapidity for the electron must be in the range  $-2.1 < \eta(\ell_e) < 2.1$
- Jet  $P_T < 45$  GeV
- The electron  $P_T$  and  $\not\!\!\!E_T$  ratio must be in the range  $0.4 < P_T/\not\!\!\!\!E_T < 1.5$

•  $\Delta \phi_{e,\not \! E_T} > 2.5.$ 

- Follow ATLAS Hadronic W/Z + MET (arXiv:1309.4017). Main backgrounds are Z > vv and W > lv
- Large radius jet, "fat jet" comes from boosted W or Z bosons, Cambridge Aachen jet algorithm
- Mass drop/filter used to examine substructure of fat jet, anti-kt jet algorithm
- Allows to differentiate from large QCD backgrounds
- MadGraph  $\rightarrow$  Pythia  $\rightarrow$  Fastjet /Delphes / Root

- $\not\!\!\!E_T > 350~{\rm GeV}$
- At least one large radius jet with  $P_T > 250 \text{ GeV}$
- $\sqrt{y} > 0.4$
- $50 < m_{jet} < 120 \text{ GeV}$
- $-1.2 < \eta < 1.2$
- No more than one narrow jet with  $P_T > 40$  GeV and  $-4.5 < \eta < 4.5$  which is separated from the leading large radius jet as  $\Delta R > 0.9$
- $\Delta \phi(jet, \not\!\!\! E_T) < 0.4$  for narrow jets.